

KLASKAMER 10

GRAAD 12 WISKUNDE: EPISODE 49

TRIGONOMETRIE 2

VRAAG 1:

Herlei elk van die volgende uitdrukkings tot 'n enkele trigonometriese verhouding:

a.
$$\frac{\sin(180^\circ - 2x) \tan(360^\circ - x) \cos(90^\circ + x)}{\sin(180^\circ - x) \tan(180^\circ + x) \sin(90^\circ - x)} \quad (5)$$

b.
$$\frac{\cos(360^\circ - 2x) + 1}{\frac{-1}{\tan(180^\circ + x)} \cdot \cos(90^\circ + x)} \quad (5)$$

BLIKslim

www.klaskamer10.co.za

TOTAAL: 10 PUNTE

VRAAG 2:

Vereenvoudig elk van die volgende deur van die **dubbel- asook saamgestelde hoekformules** gebruik te maak.

a. $\sin 165^\circ$ (4)

b. $\frac{8\sin^2 190^\circ - 8\cos^2 350^\circ}{2 \sin 250^\circ}$ (6)



TOTAAL: 10 PUNTE

GRAAD 12 WISKUNDE: EPISODE 49 (MEMORANDUM)

TRIGONOMETRIE 2

VRAAG 1:

$$\begin{aligned} \text{a. } & \frac{\sin(180^\circ - 2x) \tan(360^\circ - x) \cos(90^\circ + x)}{\sin(180^\circ - x) \tan(180^\circ + x) \sin(90^\circ - x)} \\ &= \frac{\sin 2x \checkmark (-\tan x) \checkmark (-\sin x) \checkmark}{(\sin x) (\tan x) (\cos x)} \checkmark \\ &= \frac{2 \sin x \cos x (-\tan x) (-\sin x) \checkmark}{(\sin x) (\tan x) (\cos x)} \checkmark \\ &= 2 \sin x \checkmark \end{aligned}$$

$$\begin{aligned} \text{b. } & \frac{\cos(360^\circ - 2x) + 1}{\tan(180^\circ + x)} \cdot \cos(90^\circ + x) \\ &= \frac{\cos 2x \checkmark + 1}{\tan x} \cdot (-\sin x) \checkmark \\ &= \frac{2 \cos^2 x - 1 + 1}{\sin x} \cdot (-\sin x) \checkmark \\ &= \frac{2 \cos^2 x}{\cos x} \checkmark \\ &= 2 \cos x \checkmark \end{aligned}$$

VRAAG 2:

$$\begin{aligned} \text{a. } & \sin 165^\circ \\ &= \sin 15^\circ \checkmark \\ &= \sin(45^\circ - 30^\circ) \checkmark \\ &= \sin 45^\circ \cos 30^\circ - \cos 45^\circ \sin 30^\circ \checkmark \\ &= \left(\frac{\sqrt{2}}{2}\right) \left(\frac{\sqrt{3}}{2}\right) - \left(\frac{\sqrt{2}}{2}\right) \left(\frac{1}{2}\right) \\ &= \frac{\sqrt{6} - \sqrt{2}}{4} \checkmark \end{aligned}$$

$$\begin{aligned} \text{b. } & \frac{8 \sin^2 190^\circ - 8 \cos^2 350^\circ}{2 \sin 250^\circ} \\ &= \frac{8 \sin^2 10^\circ - 8 \cos^2 10^\circ \checkmark}{-2 \sin 70^\circ \checkmark} \\ &= \frac{-8(\cos^2 10^\circ - \sin^2 10^\circ) \checkmark}{-2 \sin 70^\circ} \\ &= \frac{4 \cos 2(10^\circ) \checkmark}{\sin 70^\circ} \\ &= \frac{4 \cos 20^\circ}{\sin 70^\circ} \checkmark = \frac{4 \sin 70^\circ}{\sin 70^\circ} \\ &= 4 \checkmark \end{aligned}$$